

1) (c or 6) At $x = 2$, $x^2 + 4 = 8$. $x + k$ must equal 8 at $x = 2$; $k = 6$.

2) (b or 1) $y = (x-1)^{\frac{7}{3}}$; $y' = \frac{7}{3}(x-1)^{\frac{4}{3}}$; $y'' = \frac{28}{9}(x-1)^{\frac{1}{3}}$. The curve changes concavity at $x = 1$ only. There is one point of inflection.

3) (b) $f'(x) = 4 - \frac{4}{x^2} + \frac{1}{4} = \frac{17x^2 - 16}{4x^2}$.

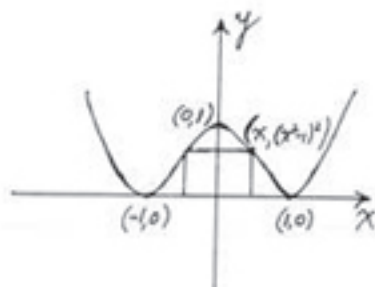
4) (d) Using the definition of the derivative of a function, $f(x) = \sqrt{x}$;

$$f'(x) = \frac{1}{\sqrt{x}}; f'(a^2) = \frac{1}{2a}.$$

5) (a or 146.563) $h = -16t^2 + 90t + 20$; $v = -32t + 90$. When $v = 0$, $t = \frac{90}{32}$.

$$h = -16\left(\frac{90}{32}\right)^2 + 90\left(\frac{90}{32}\right) + 20 = 146.563$$

6) (a or .572) $A = 2x(x^2 - 1)^2$. Using a calculator, the maximum value for A when $-1 \leq x \leq 1$ is .572. (If $x > 1$ the rectangle would not be inscribed in the given region.) Or, using



calculus, $A' = 2x(2(x^2 - 1)2x) + 2(x^2 - 1)^2 = 0$, $x = \frac{\sqrt{5}}{5}$ for max,

$$A = \frac{2}{5}\sqrt{5} \cdot \frac{16}{25} = .572.$$

7) $\left(\frac{a}{\sqrt{2}}, \frac{b}{\sqrt{2}}\right)$ $PQ = 2x$. $A = \frac{1}{2}(2x)y = xy$. $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$; $y = \frac{b}{a}\sqrt{a^2 - x^2}$.

$$A = x \cdot \frac{b}{a}\sqrt{a^2 - x^2}. \frac{dA}{dx} = \frac{b}{a}\sqrt{a^2 - x^2} + x \cdot \frac{b}{a} \cdot \frac{-x}{\sqrt{a^2 - x^2}} = 0.$$

$$\frac{dA}{dx} = a^2 - x^2 - x^2 = 0. x = \frac{a}{\sqrt{2}}, y = \frac{b}{a}\sqrt{a^2 - \frac{a^2}{2}} = \frac{b}{a} \cdot \frac{a}{\sqrt{2}} = \frac{b}{\sqrt{2}}.$$

$$Q\left(\frac{a}{\sqrt{2}}, \frac{b}{\sqrt{2}}\right) \text{ or } \left(\frac{a\sqrt{2}}{2}, \frac{b\sqrt{2}}{2}\right)$$

8) (P(2,2), R(-1,-4)) From the coordinates the slope of PR = $\frac{\frac{1}{2}a^2 + 3 + c^2}{a - c}$.

From the derivatives the slope of PR = $a = -2c$. Substituting; $\frac{\frac{1}{2}(-2c)^2 + 3 + c^2}{-2c - c} = -2c$.

$$\frac{3c^2 + 3}{-3c} = -2c; 3c^2 = 3, c = -1 \text{ (QIII)}, -3 - c^2 = -4. a = -2(-1) = 2, \frac{1}{2}2^2 = 2, P(2,2), R(-1,-4).$$

(Both coordinates must be correct to receive credit.)